

Inference at \* 2 2 1 1  
of proof for Lemma p-fun-exp-add-sq:

....equality.... NILNIL

1.  $A : \text{Type}$
2.  $f : A \rightarrow (A + \text{Top})$
3.  $x : A$
4.  $m : \mathbb{Z}$
5.  $0 < m$
6.  $\forall n : \mathbb{N}. (\uparrow \text{can-apply}(f^{\wedge} m - 1; x)) \Rightarrow ((f^{\wedge} n + (m - 1)(x)) \sim (f^{\wedge} n(\text{do-apply}(f^{\wedge} m - 1; x))))$
7.  $n : \mathbb{N}$
8.  $\uparrow \text{can-apply}(f^{\wedge} m; x)$
9.  $\neg(n = 0)$
10.  $\neg(n + m = 0)$
11.  $\neg(n = 0)$
12.  $\neg(m = 0)$

$\vdash (f \circ f^{\wedge} (n+m) - 1 (x)) \sim (f \circ f^{\wedge} n (\text{do-apply}(f^{\wedge} m - 1; x)))$   
by ((Unfold ‘p-compose‘ ( 0)·)  
CollapseTHEN (RepUR “can-apply do-apply“ ( 0)·)·)

CollapseTHEN ((Subst’ (( $n+m$ ) - 1)  $\sim$  ( $n+(m - 1)$ ) ( 0)·)  
CollapseTHEN (((Try (Complete (Auto·))·)·)  
CollapseTHEN ((Subst’ ( $f^{\wedge} n+(m - 1)(x)$ )  
 $\sim$   
( $f^{\wedge} n(\text{do-apply}(f^{\wedge} m - 1; x))$ ) ( 0)·)

CollapseTHEN (((Try ((Fold ‘do-apply‘ 0  
CollapseTHEN (Trivial)·)·)  
CollapseTHEN (if ((0) = 0) then BackThruSomeHyp else BHyp (0) )·)·)·)·

1:

$\vdash \uparrow \text{can-apply}(f^{\wedge} m - 1; x)$